

## Discussion - June 22

### Linear combinations

1. Write  $\begin{bmatrix} 3 \\ 5 \end{bmatrix}$  as a lin. comb. of  $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$  and  $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ , if possible.
2. Write  $\begin{bmatrix} 3 \\ 5 \\ -2 \end{bmatrix}$  as a lin. comb. of  $\begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$  and  $\begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$ , if possible.
3. What are all the ways  $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$  can be written as a linear combination of  $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$ ,  $\begin{bmatrix} -1 \\ -1 \end{bmatrix}$ , and  $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$ ?

### Span

1. Geometrically, describe  $\text{Span} \left\{ \begin{bmatrix} 1 \\ 1 \end{bmatrix} \right\}$ .
2. Geometrically, describe  $\text{Span} \left\{ \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 2 \\ -1 \end{bmatrix} \right\}$ .
3. What vector is always in the span of any collection of vectors in  $\mathbb{R}^n$ ?
4. What vectors  $\vec{u}, \vec{v} \in \mathbb{R}^2$  are such that  $\text{Span}\{\vec{u}, \vec{v}\} = \mathbb{R}^2$ ?  
(in other words, "which span  $\mathbb{R}^2$ "?)
5. What vectors are in  $\text{Span} \left\{ \begin{bmatrix} 0 \\ 0 \end{bmatrix} \right\}$ ?

### Logic

1. If it is raining, there are puddles on the ground.
  - a) If it is not raining, then what?
  - b) If there are puddles on the ground, then what?
  - c) If there are no puddles on the ground, then what?

} if you can conclude anything, otherwise, give a plausible scenario.
2. For every cute cat, there is a cuter cat.  
There is a cute cat, cuter than every other cat.  
Do these mean the same thing? How would you disprove them?  
(i.e., what are their logical negations?)