

Quiz 13

1. (5 points). Evaluate the indefinite integral $\int \frac{x}{1+x^2} dx$.

2. (5 points). Evaluate the definite integral $\int_1^2 t^3 \sqrt{t^2 - 1} dt$.

3. (5 points). Evaluate the indefinite integral $\int \frac{\cos 5y}{e^{\sin 5y}} dy$.

Extra credit. (2 points). Determine the area of the region between $y = \sin x$ and $y = \cos x$ on the interval $[0, \pi/2]$.

Super extra credit. (5 points). Evaluate $\int_0^1 \frac{x^4(1-x)^4}{1+x^2} dx$. Simplify the result to reach a nice conclusion (notice that the integrand is nonnegative).